

# REPORT DOCUMENTATION PAGE

Form Approved  
OMB No. 0704-0188

Public reporting burden for this collection of information is estimated to average 1 hour per response, including the time for reviewing instructions, searching existing data sources, gathering and maintaining the data needed, and completing and reviewing the collection of information. Send comments regarding this burden estimate or any other aspect of this collection of information, including suggestions for reducing this burden to Washington Headquarters Services, Directorate for Information Operations and Reports, 1215 Jefferson Davis Highway, Suite 1204, Arlington, VA 22202-4302, and to the Office of Management and Budget, Paperwork Reduction Project (0704-0188), Washington, DC 20503.

**PLEASE DO NOT RETURN YOUR FORM TO THE ABOVE ADDRESS.**

1. REPORT DATE (DD-MM-YYYY)	2. REPORT TYPE	3. DATES COVERED		
	Conference Proceeding	08-12 September 2003		
4. TITLE AND SUBTITLE		5a. CONTRACT NUMBER  5b. GRANT NUMBER  5c. PROGRAM ELEMENT NUMBER		
About Nonlinear Dependence of Remote Sensing and Diffuse Reflection Coefficients on Gordon's Parameter		5d. PROJECT NUMBER  VSF 73-6641-02-5		
6. AUTHOR(S)		5e. TASK NUMBER  5f. WORK UNIT NUMBER		
V. I. Haltrin and Sonia C. Gallegos				
7. PERFORMING ORGANIZATION NAME(S) AND ADDRESS(ES)			8. PERFORMING ORGANIZATION REPORT NUMBER	
Naval Research Laboratory Oceanography Division Stennis Space Center, MS 39529-5004			NRL/PP/7330-03-0010	
9. SPONSORING/MONITORING AGENCY NAME(S) AND ADDRESS(ES)			10. SPONSOR/MONITOR'S ACRONYM(S)	
Office of Naval Research 800 N. Quincy St. Arlington, VA 22217-5660			ONR	
			11. SPONSOR/MONITOR'S REPORT NUMBER(S)	
12. DISTRIBUTION/AVAILABILITY STATEMENT				
Approved for public release; distribution is unlimited				
13. SUPPLEMENTARY NOTES				
20031217 280				
14. ABSTRACT				
Remote sensing $i$ - and diffuse reflection $R$ coefficients of seawater are dependent on inherent optical properties of seawater through the Gordon's parameter $bB$ / (a $bB$ ), where $a$ is an absorption and $b$ is backscattering coefficients. $g = +B$ Majority of researchers in ocean optics use linear approximation for $i$ and $R$ , i. e. $i \sim g$ and $R \propto g$ . This approach works well when $g \sim 0.1$ . All open and largest part of coastal waters satisfy this condition, but there are some cases when parameter $g$ is as large as 0.98. We illustrate this fact with a histogram of Gordon's parameter $g$ for the Yellow sea waters. We present a choice of alternative rigorous nonlinear equations for $R$ that solve this problem, i.e. significantly reduce the error of the restoration of the Gordon's parameter $g$ from remote sensing optical data and estimate possible errors in using linear dependencies				
15. SUBJECT TERMS				
nonlinear, remote sensing, diffuse reflection, Gordon's parameter				
16. SECURITY CLASSIFICATION OF:		17. LIMITATION OF ABSTRACT	18. NUMBER OF PAGES	19a. NAME OF RESPONSIBLE PERSON
a. REPORT	b. ABSTRACT	c. THIS PAGE		Vladimir Haltrin
Unclassified	Unclassified	Unclassified	SAR	19b. TELEPHONE NUMBER (Include area code) 228-688-4528
Standard Form 298 (Rev. 8/98) Prescribed by ANSI Std. Z39-18				

## PUBLICATION OR PRESENTATION RELEASE REQUEST

Pubkey: 3717

NRLINST 5600.2

REFERENCES AND ENCLOSURES		2. TYPE OF PUBLICATION OR PRESENTATION		3. APPROVAL	
		<input type="checkbox"/> Abstract only, published <input type="checkbox"/> Book <input type="checkbox"/> Conference Proceedings (refereed) <input type="checkbox"/> Invited speaker <input type="checkbox"/> Journal article (refereed) <input type="checkbox"/> Oral Presentation, published <input type="checkbox"/> Other, explain		<input type="checkbox"/> Abstract only, not published <input type="checkbox"/> Book chapter <input checked="" type="checkbox"/> Conference Proceedings (not refereed) <input type="checkbox"/> Multimedia report <input type="checkbox"/> Journal article (not refereed) <input type="checkbox"/> Oral Presentation, not published	
Ref: (a) NRL Instruction 5600.2 (b) NRL Instruction 5510.40D				STRN <u>NRL/PP/7330-03-10</u>	
Encl: (1) Two copies of subject paper (or abstract)				Route Sheet No. <u>7330/</u>	
				Job Order No. <u>73-8028-B3-5</u>	
				Classification <u>X</u> U <u>C</u>	
				Sponsor <u>ONR BASE</u>	
				approval obtained <input checked="" type="checkbox"/> yes <input type="checkbox"/> no	

## 4. AUTHOR

Title of Paper or Presentation

About Nonlinear Dependence of Remote Sensing and Diffuse Reflection Coefficients on Gordon's Parameter

Author(s) Name(s) (First, MI, Last), Code, Affiliation if not NRL

Vladimir I. Haltrin Sonia C. Gallegos

It is intended to offer this paper to the 2nd Int. ONW Conference

(Name of Conference)

18-SEP - 12-SEP-2003, St. Petersburg, Russia, Unclassified

(Date, Place and Classification of Conference)

and/or for publication in 2nd Int. ONW Conference, Unclassified

(Name and Classification of Publication)

(Name of Publisher)

After presentation or publication, pertinent publication/presentation data will be entered in the publications data base, in accordance with reference (a).

It is the opinion of the author that the subject paper (is       ) (is not   X  ) classified, in accordance with reference (b).This paper does not violate any disclosure of trade secrets or suggestions of outside individuals or concerns which have been communicated to the Laboratory in confidence. This paper (does       ) (does not   X  ) contain any militarily critical technology. This subject paper (has       ) (has never   X  ) been incorporated in an official NRL Report.

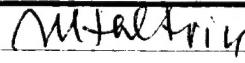
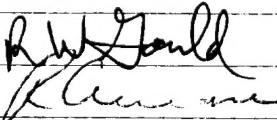
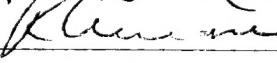
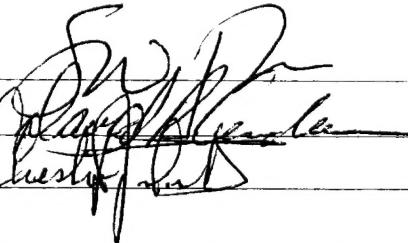
Vladimir I. Haltrin, 7333

Name and Code (Principal Author)



(Signature)

## 5. ROUTING/APPROVAL

CODE	SIGNATURE	DATE	COMMENTS
Author(s) Haltrin		7/16/03	Abstract to this paper is already signed
Section Head Gould, acting		7/16/03	
Branch Head Arnone		7/18/03	
Division Head Payne, acting		7/17/03	
Security, Code 7030.1		7/18/03	1. Release of this paper is approved.
Office of Counsel, Code 1008.3		7/21/03	2. To the best knowledge of this Division, the subject matter of this paper (has <u>      </u> ) (has never <u>  X  </u> ) been classified.
ADOR/Director NCST E.O. Hartwig, 7000			1. Paper or abstract was released.
Public Affairs (Unclassified/ Unlimited Only), Code 7030.4			2. A copy is filed in this office. <u>SSC-281-3</u>
Division, Code			
Author, Code			

A - Approved for public release, distribution is unlimited.

B - Distribution authorized to U.S. Government agencies only (check reason below):

<input type="checkbox"/> Foreign Government Information	<input type="checkbox"/> Contractor Performance Evaluation
<input type="checkbox"/> Proprietary Information	<input type="checkbox"/> Administrative/Operational Use
<input type="checkbox"/> Test and Evaluation	<input type="checkbox"/> Software Documentation

<input type="checkbox"/> Critical Technology
<input type="checkbox"/> Premature Dissemination
<input type="checkbox"/> Cite "Specific Authority" _____ (Identification of valid documented authority)

Date statement applied \_\_\_\_\_

Other requests for this document shall be referred to \_\_\_\_\_  
(Insert Controlling DOD Office\*)

C - Distribution authorized to U.S. Government agencies and their contractors (check reason below):

<input type="checkbox"/> Foreign Government Information	<input type="checkbox"/> Software Documentation
<input type="checkbox"/> Administrative/Operational Use	<input type="checkbox"/> Critical Technology

<input type="checkbox"/> Cite "Specific Authority" _____ (Identification of valid documented authority)
--

Date statement applied \_\_\_\_\_

Other requests for this document shall be referred to \_\_\_\_\_  
(Insert Controlling DOD Office\*)

D - Distribution authorized to DOD and DOD contractors only (check reason below):

<input type="checkbox"/> Foreign Government Information	<input type="checkbox"/> Critical Technology
<input type="checkbox"/> Software Documentation	<input type="checkbox"/> Cite "Specific Authority" _____ (Identification of valid documented authority)
<input type="checkbox"/> Administrative/Operational Use	

Date statement applied \_\_\_\_\_

Other requests for this document shall be referred to \_\_\_\_\_  
(Insert Controlling DOD Office\*)

E - Distribution authorized to DOD components only (check reason below):

<input type="checkbox"/> Proprietary Information	<input type="checkbox"/> Premature Dissemination
<input type="checkbox"/> Foreign Government Information	<input type="checkbox"/> Software Documentation
<input type="checkbox"/> Administrative/Operational Use	<input type="checkbox"/> Contractor Performance Evaluation

<input type="checkbox"/> Critical Technology
<input type="checkbox"/> Direct Military Support
<input type="checkbox"/> Test and Evaluation
<input type="checkbox"/> Cite "Specific Authority" _____ (Identification of valid documented authority)

Date statement applied \_\_\_\_\_

Other requests for this document shall be referred to \_\_\_\_\_  
(Insert Controlling DOD Office\*)

F - Further dissemination only as directed by \_\_\_\_\_

(Insert Controlling DOD Office\*)

Date statement applied \_\_\_\_\_

or higher DOD authority \_\_\_\_\_

G - Distribution authorized to U.S. Government agencies and private individuals or enterprises eligible to obtain export-controlled technical data in accordance with regulations implementing 10 U.S.C. 140c.

Date statement applied \_\_\_\_\_

Other requests for this document shall be referred to \_\_\_\_\_  
(Insert Controlling DOD Office\*)

\*For NRL publications, this is usually the Commanding Officer, Naval Research Laboratory, Washington, DC 20375-5320

#### 7 OTHER LIMITATION

Classification       NOFORN       DTIC exempt (explain) \_\_\_\_\_

Classification Review  
(initial/Date)

Substantive changes made in this document after approval by Classification Review and Public Release invalidate these reviews. Therefore, if any substantive changes are made by the author, Technical Information, or anyone else, the document must be returned for another Classification Review and Publication Release.

#### 8 INSTRUCTIONS

Author completes and submits this form with the manuscript via line channels to the division head for review and approval according to the routing in Section 4.

1. NRL Reports.....Submit the diskette (if available), manuscript, typed double-spaced, complete with tables, illustrations, references, draft SF 298, and proposed distribution list.
2. NRL Memorandum Reports.....Submit a copy of the original, typed manuscript complete with tables, illustrations, references, draft SF 298, and proposed distribution list.
3. NRL Publications or other books, brochures, pamphlets, proceedings, or any other printed publications.....Handled on a per case basis by Site Technical Information Office.

## **ABOUT NONLINEAR DEPENDENCE OF REMOTE SENSING AND DIFFUSE REFLECTION COEFFICIENTS ON GORDON'S PARAMETER**

Vladimir I. Haltrin, and Sonia C. Gallegos

Naval Research Laboratory, Ocean Optics Section, Code 7333,  
Stennis Space Center, MS 39529-5004, USA

e-mail: haltrin@nrlssc.navy.mil, web page: <http://haltrin.freeshell.org>

**Abstract:** Remote sensing  $r_{rs}$  and diffuse reflection  $R$  coefficients of seawater are dependent on inherent optical properties of seawater through the Gordon's parameter  $g = b_B / (a + b_B)$ , where  $a$  is an absorption, and  $b_B$  is backscattering coefficients. Majority of researchers in ocean optics use linear approximation for  $r_{rs}$  and  $R$ , i.e.  $r_{rs} \propto g$  and  $R \propto g$ . This approach works well when  $g \leq 0.1$ . All open and largest part of coastal waters satisfy this condition, but there are some cases when parameter  $g$  is as large as 0.98. We illustrate this fact with a histogram of Gordon's parameter  $g$  for the Yellow sea waters. We present a choice of alternative rigorous nonlinear equations for  $R$  that solve this problem, i.e. significantly reduce the error of the restoration of the Gordon's parameter  $g$  from remote sensing optical data and estimate possible errors in using linear dependencies

### **1. Introduction**

Diffuse reflection coefficient (DRC) of water body is an informative part of remote sensing reflectance [1] of light by the ocean. DRC contains information on content of dissolved and suspended substances in seawater. DRC is an apparent optical property that depends not only on inherent optical properties of the seawater, but also on the parameters of illumination. The dependence on inherent optical properties is expressed through the dependence on Gordon's parameter, i.e. the ratio of backscattering coefficient  $b_B$  to the sum of absorption  $a$  and backscattering coefficient,  $g = b_B / (a + b_B)$ . In the open ocean DRC is linearly proportional to  $g$ . This linear equation is very good for the Type I open ocean waters [2]. It is also acceptable for about 90% of coastal waters. Theoretical and numerical analysis show that the linear relationship can be adequately used only when Gordon's parameter  $g$  is relatively small, i.e.  $g < 0.1$ . This criterion is always satisfied in open ocean waters. The available database of experimental measurements show that in coastal waters Gordon's parameter may exceed this critical value of 0.1. In some very turbid coastal waters it can even reach values higher than 0.95. For example, in waters of Yellow Sea or coastal waters close to river estuaries the percentage of cases when  $g > 0.1$  can reach 50% or more. In this paper we illustrate this fact with a histogram of Gordon's parameter for the Yellow sea waters. We estimate possible errors in using the linear dependence and present a choice of alternative rigorous nonlinear equations for DRC that solve this problem, i.e. significantly reduce the error of the restoration of the Gordon's parameter from remote sensing optical data.

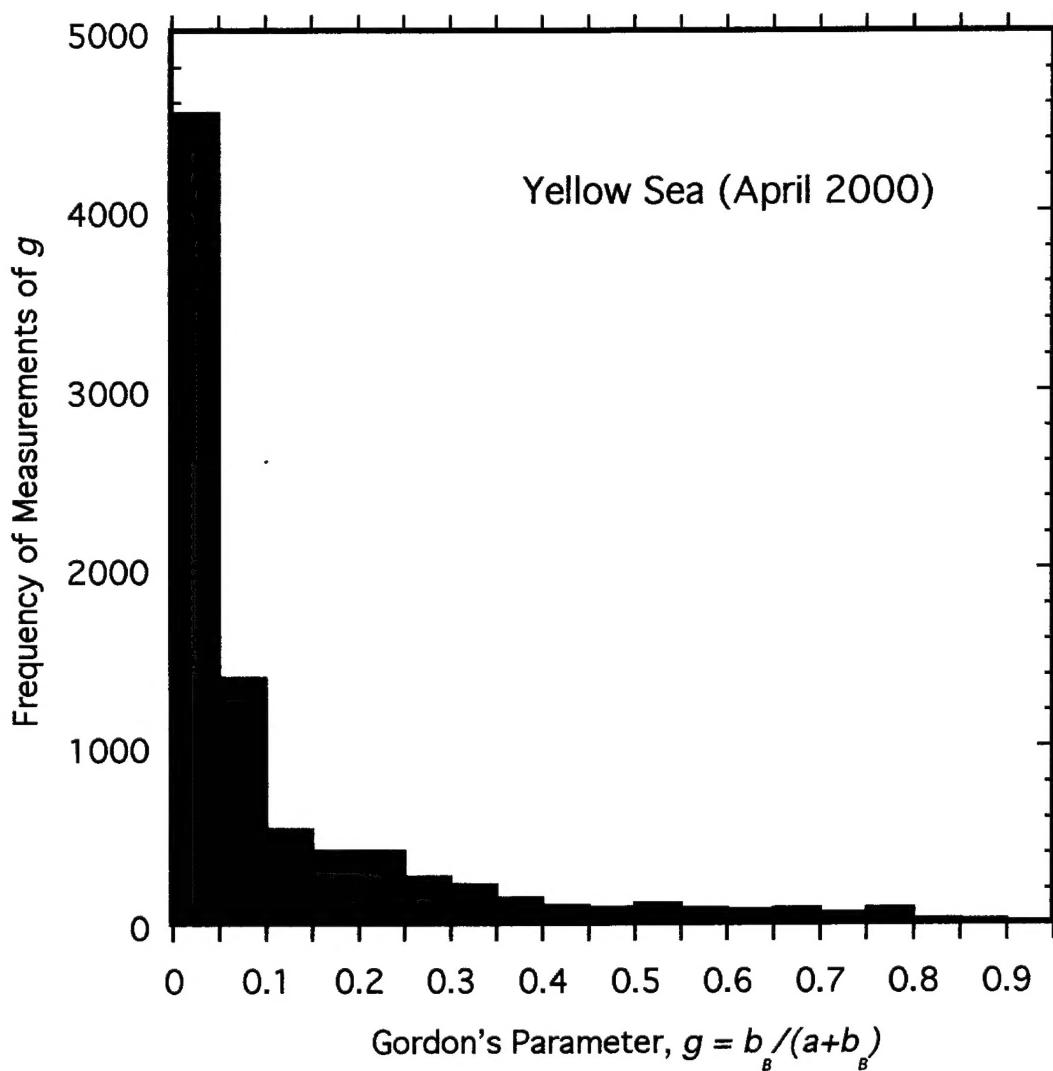


Figure 1. Distribution of occurrences of measured Gordon's parameter in Yellow Sea in 2000.

## 2. Gordon's parameter in highly scattering marine environment

Until recently we had no significant cases of *in situ* measurements that show existence of sea waters with high cases of Gordon's parameter  $g$  exceeding 0.1. Relatively recent measurements made in 2000 by NRL researches with collaboration of Korean scientists in Yellow Sea shows that these highly scattering waters exhibit these characteristics. Figure 1 shows a histogram of the frequency of measurements of Gordon's parameter in this expedition. In this case more than 50% of measurements correspond to Gordon's parameter exceeding critical limit of linear approach. It means that processing of such data should involve nonlinear equations connecting DRC with  $g$ .

### 3. Equations for diffuse reflectance that valid for all values of Gordon's parameter

Fortunately, we have both experimental data and theoretical equations that correctly connect diffuse reflection coefficient with Gordon's parameter  $g$ , and, consequently, with  $a$  and  $b_B$  for the full range of their variability,  $0 \leq g \leq 1$ ,  $0 \leq a \leq \infty$ ,  $0 \leq b_B \leq \infty$ . First, we have experimental data published by Timofeyeva in 1972 and 1979 [3, 4] (see Tab. 1). Second, we have several equations that connect DRC with  $g$  in the full range of variability of this parameter,  $0 \leq g \leq 1$ . Let us consider these cases.

Table 1. Optical properties of natural and modeled scattering and absorbing media according to experiments by Timofeyeva. Here  $\bar{\mu}$ ,  $\bar{\mu}_d$ , and  $\bar{\mu}_u$  are, correspondingly, total, downward, and upward average cosines over radiance distribution in the scattering medium [5].

$\bar{\mu}$	$\bar{\mu}_d$	$\bar{\mu}_u$	$R$	$g$	$R/g$
0	0.5	0.5	1.0	1.0	1.0
0.1	0.5249	0.4831	0.671	0.9408	0.7132
0.2	0.5525	0.4545	0.443	0.7970	0.5550
0.3	0.5834	0.4202	0.283	0.6179	0.4580
0.4	0.6184	0.3745	0.171	0.4439	0.3852
0.5	0.6566	0.3311	0.095	0.2959	0.3211
0.6	0.7008	0.3003	0.048	0.1802	0.2664
0.7	0.7536	0.2857	0.0207	0.0967	0.2141
0.8	0.8217	0.3610	0.0082	0.0413	0.1985
0.9	0.9033	0.6849	0.0016	0.0101	0.1584
1.0	1.0	1.0	0.0	0.0	0.25

a) Equation derived from the exact solution of radiative transfer equation in the depth of scattering medium [6]:

$$R = \frac{1-\eta}{1+\eta} \left( \sqrt{1+\eta^2} - \eta \right)^2, \quad \eta = \sqrt{\frac{1-g}{1+(3+2\sqrt{2})g}} = \sqrt{\frac{a}{a+2(2+\sqrt{2})b_B}}. \quad (1)$$

b) Equation derived in the framework of self-consistent approach [5] (asymptotic case):

$$R_\infty = \left( \frac{1-\bar{\mu}}{1+\bar{\mu}} \right)^2, \quad (2)$$

$$\bar{\mu} = \sqrt{\frac{1+2g-\sqrt{g(4+5g)}}{1+g}} = \sqrt{\frac{a}{a+3b_B+\sqrt{b_B(4a+9b_B)}}}. \quad (3)$$

c) Equation derived in the framework of self-consistent approach [5] (case of diffuse illumination):

$$R = \frac{2(1-\bar{\mu})^2}{\bar{\mu}(3-\bar{\mu}^2)} \left\{ 1 - \frac{1+\bar{\mu}^2}{\bar{\mu}(3-\bar{\mu}^2)} \ln \left[ 1 + \frac{\bar{\mu}(3-\bar{\mu}^2)}{1+\bar{\mu}^2} \right] \right\}, \quad (4)$$

here  $\bar{\mu}$  is defined by Eq. (3).

d) Equation derived in the framework of semi-empirical approach [7] that is based on experimental data presented in Tab. 1:

$$R = \frac{1-\bar{\mu}/\mu_d}{1+\bar{\mu}/\mu_u}, \quad (5)$$

here

$$\bar{\mu} = a_0 + (1-a_0) \sqrt{1-g} + \sum_{n=1}^6 a_n g^{\frac{n}{3}}, \quad (6)$$

$$\mu_d = \left[ 1 - \bar{\mu} (1 - \bar{\mu})^2 \sum_{n=0}^3 b_n \bar{\mu}^{2n} \right] / (2 - \bar{\mu}), \quad (7)$$

$$\mu_u = \left[ 1 - \bar{\mu} (1 - \bar{\mu})^2 \exp \left( \sum_{n=0}^4 c_n \bar{\mu}^{2n} \right) \right] / (2 - \bar{\mu}). \quad (8)$$

The coefficients  $a_n$ ,  $b_n$  and  $c_n$  in Eqs. (5-8) are given in Tab. 2.

Table 2. Coefficients to Eqs. (5)-(8).

n	$a_n$	$b_n$	$c_n$
0	0.5918	0.0326	-0.0131
1	-0.7937	0.1661	8.4423
2	4.8350	0.7785	-15.6605
3	-22.8150	0.0228	21.8820
4	42.6859		-11.2257
5	-35.8945		
6	11.3905		

Equations (1)-(8) are valid for the full range of variability of parameters  $g$ ,  $a$ , and  $b_B$ :  $0 \leq g \leq 1$ ,  $0 \leq a \leq \infty$ ,  $0 \leq b_B \leq \infty$ . In order to make a comparison and estimate possible errors for the case presented in Fig. 1 we will use also the following equation used in ocean optics research:

e) Linear equation by Morel and Prieur [2]:

$$R = g / 3. \quad (9)$$

Linear equation (9) was never meant to be used by authors in the full range of variability of  $g$ . It was proposed for the case of open ocean waters where  $g$  is small.

f) Kubelka-Munk equation [8]:

$$R = \left(1 - \sqrt{1 - g^2}\right) / g. \quad (10)$$

Equation (10) was derived in the assumption that  $\bar{\mu}_d = \bar{\mu}_u = 0.5$ . Because in seawater both  $\bar{\mu}_d$  and  $\bar{\mu}_u$  are far from 0.5 (see Tab. 1) that equations is not good for marine optics except special cases with  $g > 0.6$ .

g) Equation by Gordon *et al.* [9] for directed sun illumination:

$$R = 0.0001 + 0.3244 g + 0.1425 g^2 + 0.1308 g^3, \quad (0.1 \leq g \leq 0.5). \quad (11)$$

g) Equation by Gordon *et al.* [9] for diffuse illumination:

$$R = 0.0003 + 0.3687 g + 0.1802 g^2 + 0.0740 g^3, \quad (0.1 \leq g \leq 0.5). \quad (12)$$

Dependencies of DRC on Gordon's parameter  $g$  computed according to Eqs. (1), (2), (4), (5), and (10)-(12) are shown in Fig. 2. Equations (1), (2), (4), and (5) give quite similar results and are valid for the whole range of  $0 \leq g \leq 1$ .

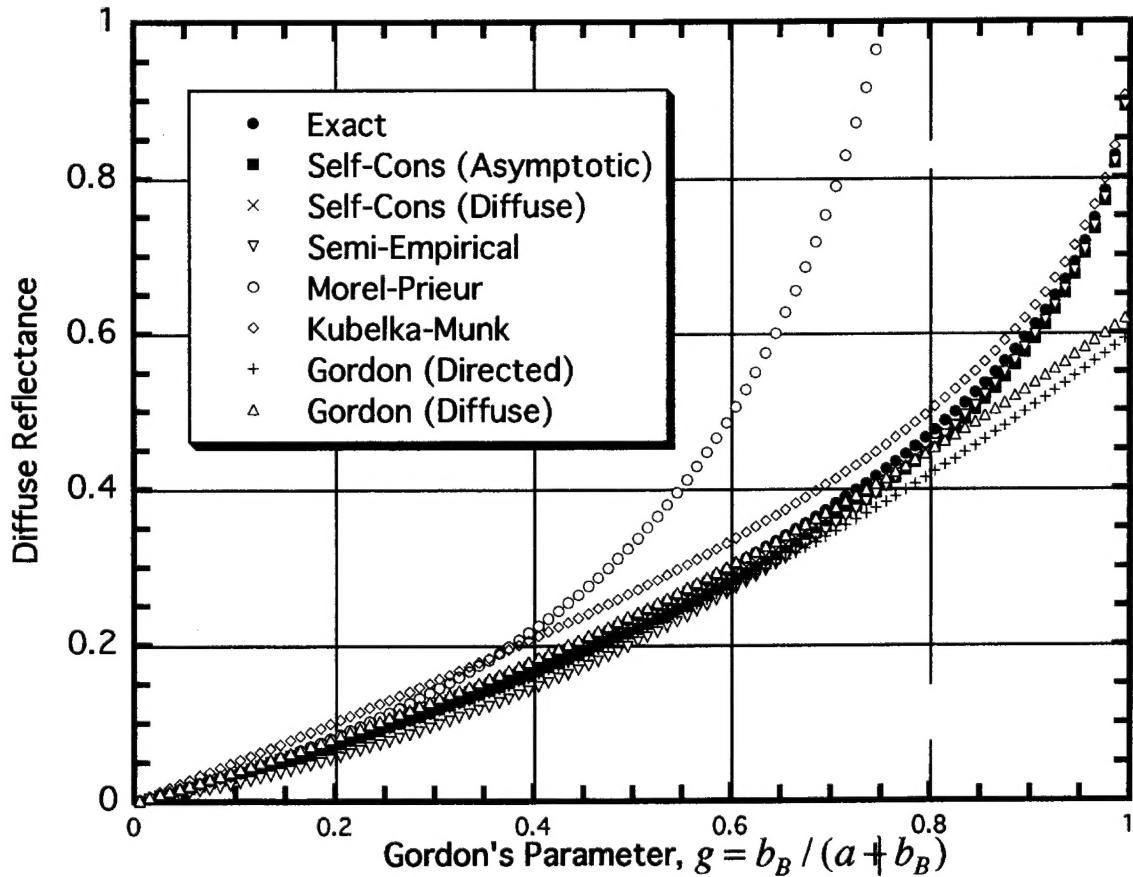


Figure 2. Dependence of Diffuse Reflectance Coefficient Gordon's parameter.

#### 4. Possible errors of using linear equations in highly-scattering waters

In order to estimate possible errors to compute diffuse reflection coefficient as a "precise" reference we used values of  $R$  as a function of  $g$  generated numerically by Hydrolight [10, 11] for the case of diffuse illumination of sea surface. The error distributions for Eqs. (2), (4), (5), and (10)-(12) are shown in Fig. 3. Because the errors of Eq. (1) for the case of diffuse illumination is much smaller, we omitted its dependence from Fig. 3.

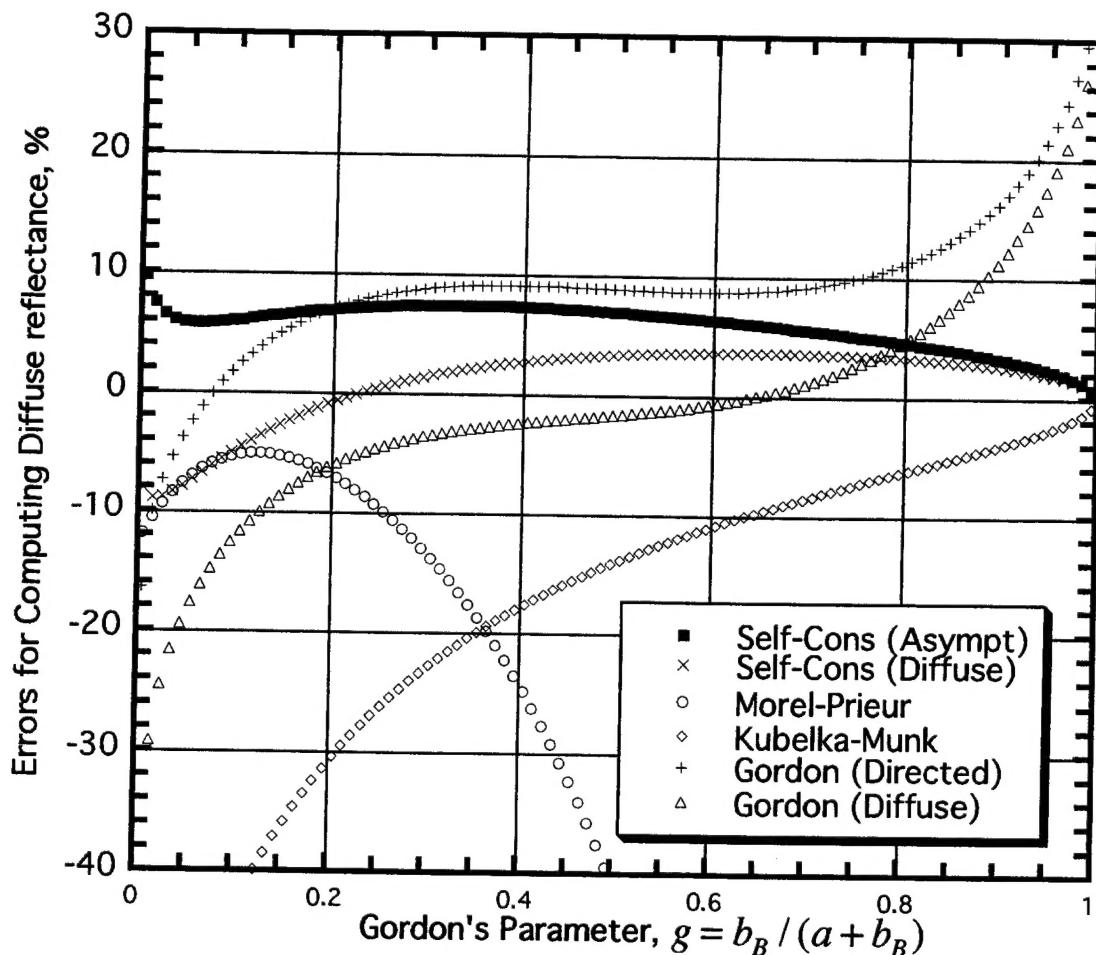


Figure 3. Error distribution for various equations to compute diffuse reflectance.

#### 4. Conclusion

The use of linear Eq. (9) is restricted to open ocean waters and coastal waters with  $g \leq 0.1$ . Equation (10) is not adequate for clean ocean waters, and Eqs. (11)-(12) are good only for typical ocean waters excluding very turbid and extremely clean waters [12]. In order to maintain 10% accuracy for the whole range of variability of optical properties of seawater we should use nonlinear Eqs. (1), (2), (4), and (5). The choice of equation should depend on the problem involved because they are related to the different theories.

## 5. Acknowledgments

The authors thank continuing support at the Naval Research Laboratory (NRL) through the VSF 73-6641-02-5 and HS 73-8028-B2 programs. This article represents NRL contribution PP-7330-03-0010.

## 6. References

1. J. V. R. Zaneveld, "A theoretical derivation of the dependence of the remotely sensed reflectance of the ocean on the inherent optical properties," *J. Geophys. Res.*, **100**, 13,135-13,142 (1995).
2. A. Morel, L. Prieur, "Analysis of variations in ocean color," *Limnol. Oceanogr.*, **22**, 709-722 (1977).
3. V. A. Timofeyeva, "Relation Between the Optical Coefficients in Turbid Media," *Izvestiya, Atmos. Ocean Physics*, **8**, pp. 654-656, (1972).
4. V. A. Timofeyeva, "Determination of Light-Field Parameters in the Depth Regime from Irradiance Measurements," *Izvestiya, Atmos. Ocean Physics*, **15**, 774-776, (1979).
5. V. I. Haltrin, "Self-consistent approach to the solution of the light transfer problem for irradiances in marine waters with arbitrary turbidity, depth and surface illumination: I. Case of absorption and elastic scattering," *Appl. Optics*, **37**, 3773-3784 (1998).
6. V. I. Haltrin, "Exact solution of the characteristic equation for transfer in the anisotropically scattering and absorbing medium." *Appl. Optics*, **27**, 599-602, (1988).
7. V. I. Haltrin, "Empirical algorithms to restore a complete set of inherent optical properties of sea water using any two of these properties," *Canadian Journal of Remote Sensing*, **26**, 440-445, (2000).
8. P. Kubelka and F. Munk. "Ein Beitrag zur Optik der Farbanstriche," *Zeit. Techn. Phys.*, **12**, 593-607 (1931).
9. H. R. Gordon, O. B. Brown, and M. M. Jacobs, "Computed relationships between the inherent and apparent optical properties of a flat homogeneous ocean," *Appl. Optics*, **14**, 417-427 (1975).
10. C. D. Mobley, *Light and Water* (Academic Press, San Diego-Toronto, 1994).
11. C. D. Mobley, and L. K. Sundman, *Hydrolight 4.1 User Guide*, Sequoia Scientific, Inc., Redmond, WA, 85 pp. (2000).
12. The defect in Eqs. (11)-(12) consists of non zero values at  $g = 0$  due to the formal use of regression analysis. The initial unpublished data of Ref. [9] is good for the case of extremely clear water too.